台大地理系：空間分析
NTU Geography: Spatial Analysis

用R進行資料分析

Data Analysis with R

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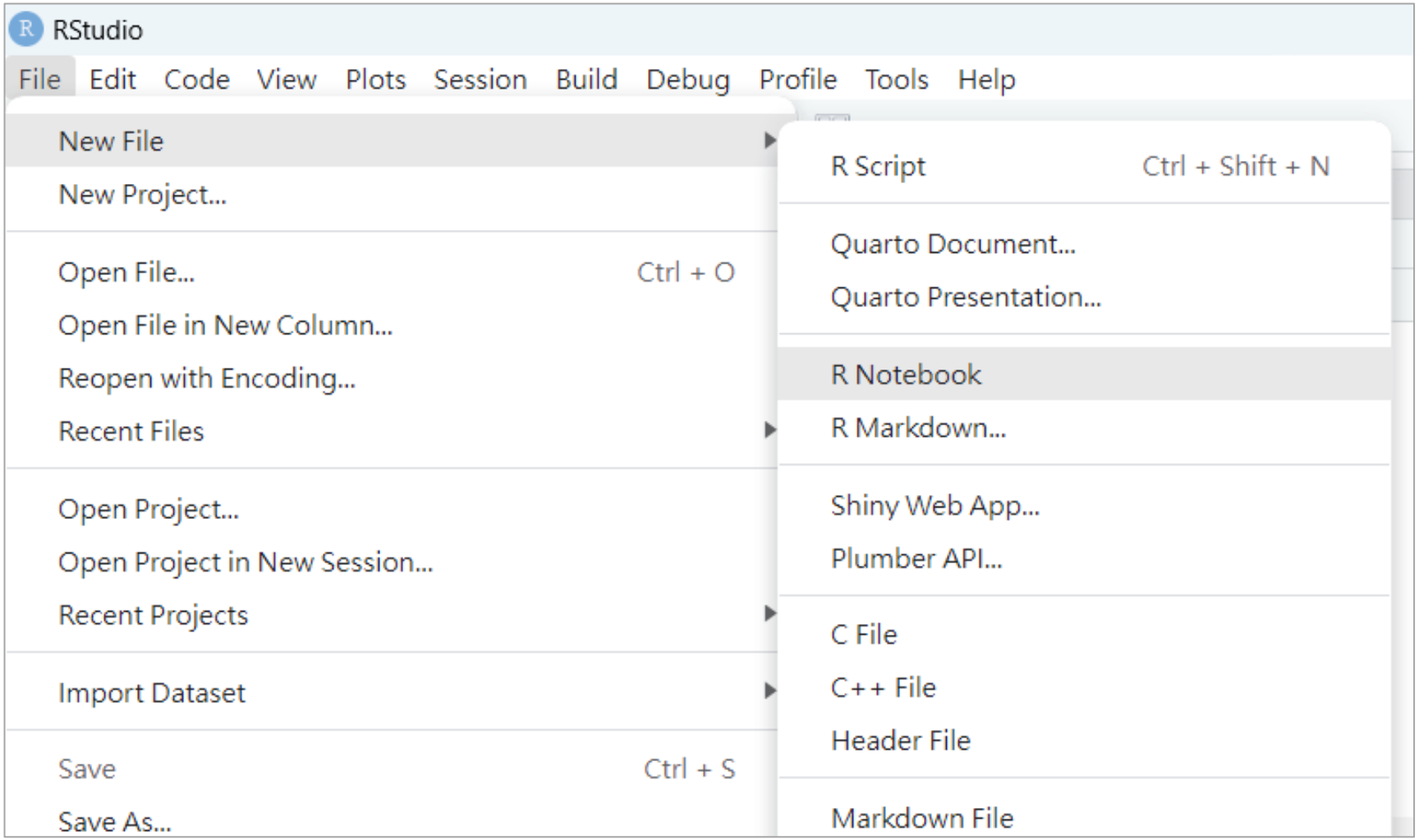
本週大綱

- 假設檢定
- 機率分布
- 統計圖表

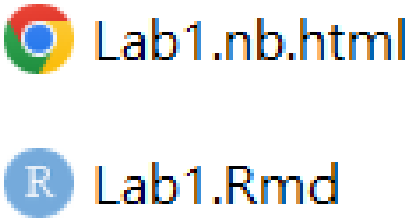
Creating R Notebook files



R Notebook files

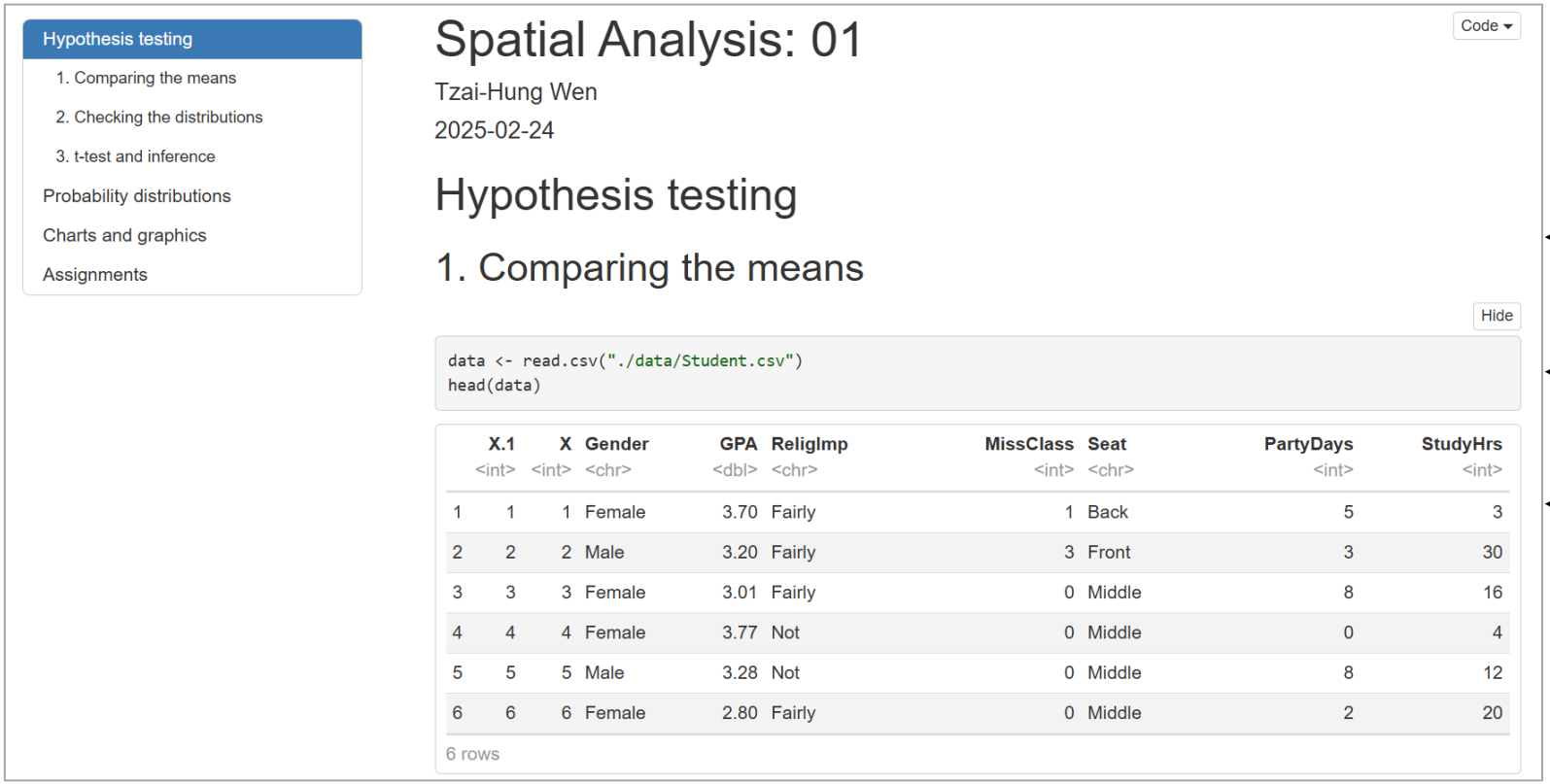
Source Visual

```
1  ---
2  title: "Spatial Analysis: 01"
3  author: "Tzai-Hung Wen"
4  date: '2025-02-24'
5  output:
6    html_notebook:
7      toc: true
8      toc_depth: 6
9      toc_float: true
10 ---
```



An R Notebook is an R Markdown document with chunks that can be executed *independently* and *interactively*, with output visible *immediately* beneath the input.

1. 假設檢定



Hypothesis testing
1. Comparing the means
2. Checking the distributions
3. t-test and inference
Probability distributions
Charts and graphics
Assignments

Code

Spatial Analysis: 01

Tzai-Hung Wen

2025-02-24

Hypothesis testing

1. Comparing the means

Hide

```
data <- read.csv("./data/Student.csv")
head(data)
```

	X.1 <int>	X <int>	Gender <chr>	GPA <dbl>	ReligImp <chr>	MissClass <int>	Seat <chr>	PartyDays <int>	StudyHrs <int>
1	1	1	Female	3.70	Fairly	1	Back	5	3
2	2	2	Male	3.20	Fairly	3	Front	3	30
3	3	3	Female	3.01	Fairly	0	Middle	8	16
4	4	4	Female	3.77	Not	0	Middle	0	4
5	5	5	Male	3.28	Not	0	Middle	8	12
6	6	6	Female	2.80	Fairly	0	Middle	2	20

6 rows

← text

← code

← output

Hypothesis Tests for Means

1. Determine the null and alternative hypotheses.
2. Verify necessary data conditions, and if met, summarize the data into an appropriate test statistic.
3. Assuming the null hypothesis is true, find the *p*-value.
4. Decide whether or not the result is statistically significant based on the *p*-value.
5. Report the conclusion in the context of the situation.

Key Concepts of Hypothesis Testing

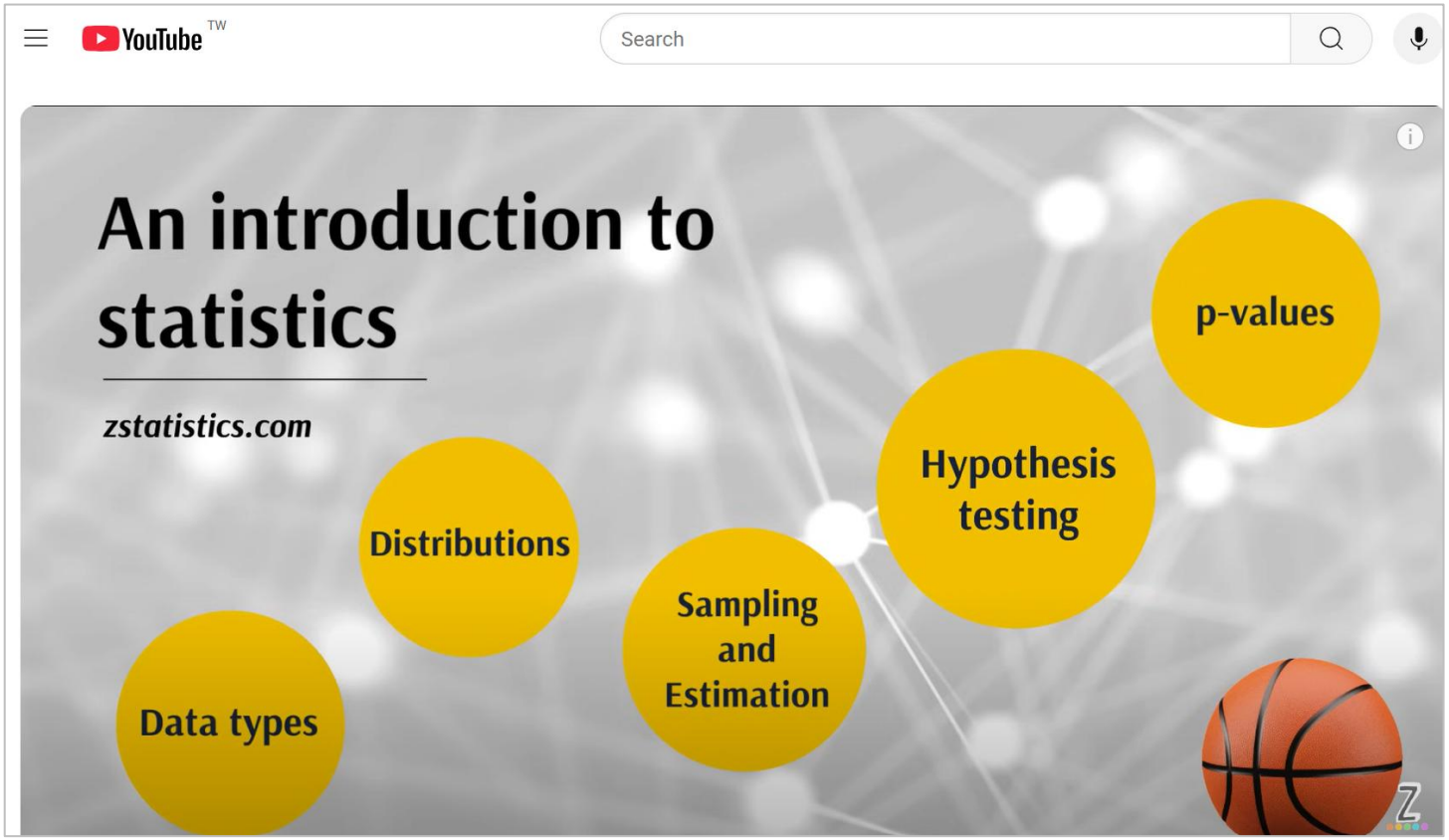
- t-distribution
- Sampling distribution
- Standard error
- Null / alternative hypothesis
- One-tailed / two-tailed test
- Significance level (e.g. alpha = 5%)
- Confidence interval (e.g. 95% C.I.)
- p-value
- Type I and Type II errors

Basic Statistics Review

https://online.stat.psu.edu/statprogram/reviews/statistical-concepts

Basic Statistics Review

https://www.youtube.com/watch?v=kyjlxsLW1Is
(42:08)



Two-sample t-test

```
t.test(GPA_Back, GPA_Front) # two tailed test
```

```
    Welch Two Sample t-test

data:  GPA_Back and GPA_Front
t = -3.1562, df = 273.52, p-value = 0.001777
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 -0.28296881 -0.06556891
sample estimates:
mean of x mean of y
 3.077015  3.251284
```

2. 機率分布

Binomial Random Variables

Conditions for a binomial experiment:

1. There are ***n* "trials"** where *n* is determined in advance and is not a random value.
2. **Two possible outcomes** on each trial, called "success" and "failure" and denoted S and F.
3. **Outcomes are independent** from one trial to the next.
4. **Probability of a "success"**, denoted by *p*, remains **same** from one trial to the next. Probability of "failure" is $1 - p$.

A **binomial random variable** is defined as *X*=number of successes in the *n* trials of a binomial experiment.

Binomial Probability Distribution

Finding Binomial Probabilities

$$P(X = k) = \frac{n!}{k!(n-k)!} p^k (1-p)^{n-k} \quad \text{for } k = 0, 1, 2, \ldots, n$$

Probability of Two Wins in Three Plays

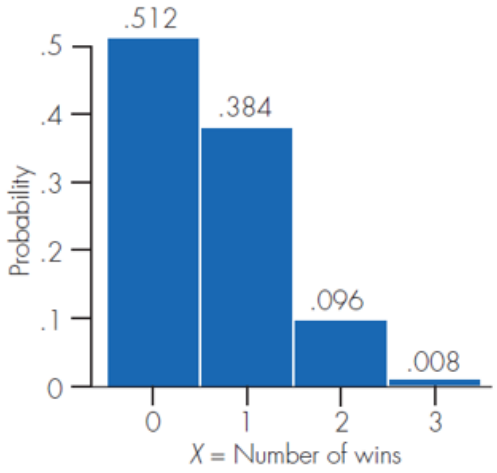
p = probability win = 0.2; plays of game are *independent*.

***X* = number of wins in three plays.**

What is ***P*(*X* = 2)**?

$$P(X = 2) = \frac{3!}{2!(3-2)!} .2^2 (1-.2)^{3-2}$$

$$= 3(.2)^2(.8)^1 = 0.096$$



Creating Binomial Prob. Distributions

- 例題：某網購公司規定消費者在一週內(7 days)購買商品可全額退款。根據過去記錄，平均每週會有2件退貨商品。
- 請繪製該公司在1個月內(30 days)退貨商品數量的機率分布圖 (probability distribution function, PDF)。
- 估計一個月的退貨商品數超過10件的機率。

Built-in functions

Binomial

dbinom(x, size, prob): prob density of x

pbinom(x, size, prob): p(<= x)

qbinom(p, size, prob): quantile function

rbinom(n, size, prob): generates random deviates

Normal

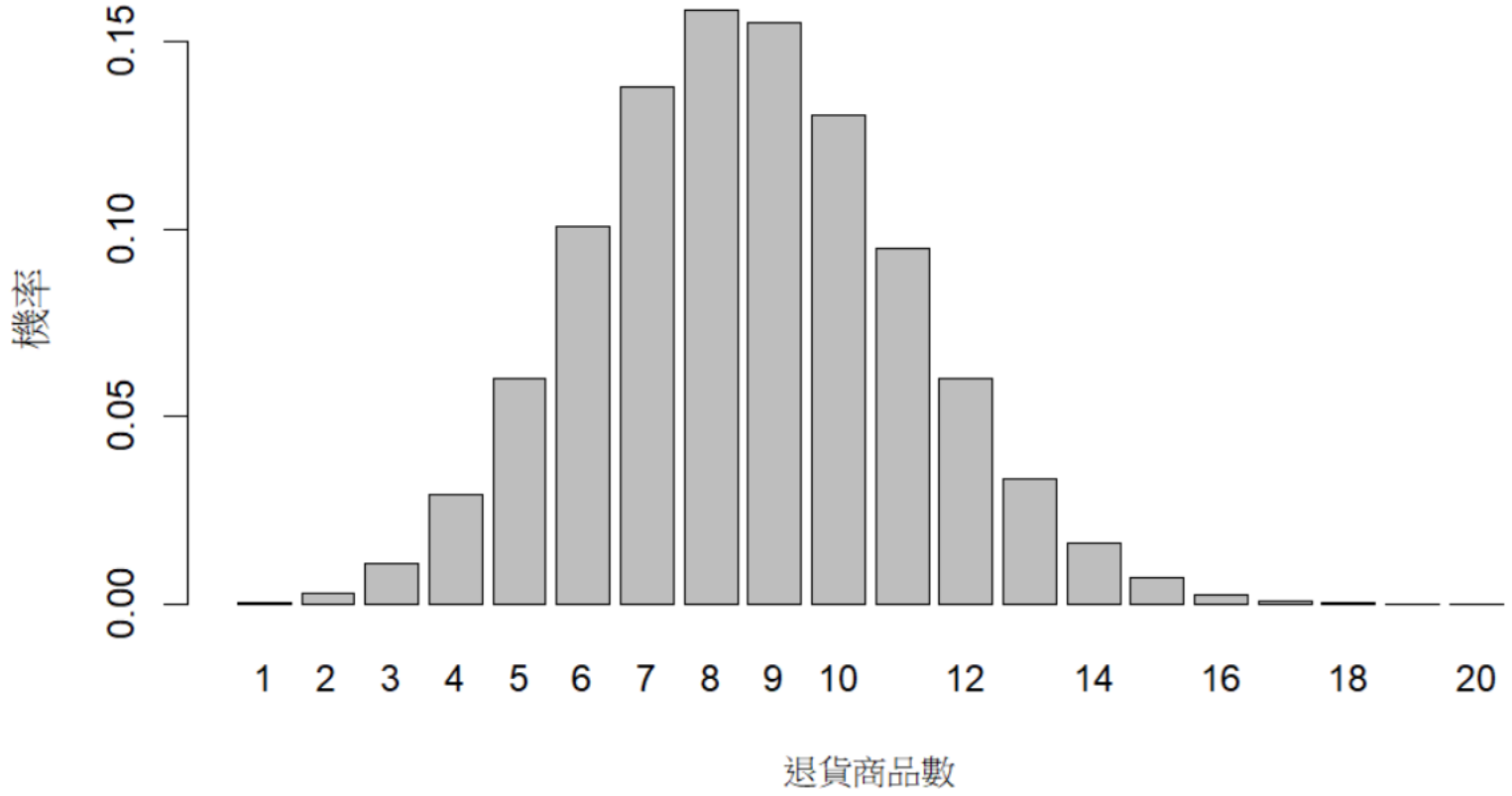
```
pnorm(35, mean=30, sd=5)      # CDF, P(x<=35)
dnorm(35, mean=30, sd=5)      # Likelihood, P(x=35)
qnorm(0.7, mean=100, sd=15) # given exceedance prob. --> x
rnorm(20, mean=100, sd=15)   # generating samples
```

```
> p = pbinom(10, size=30, prob= 2/7) # prob(X <=10)
> pGT10 <- 1 - p
> pGT10
[1] 0.2146092
```

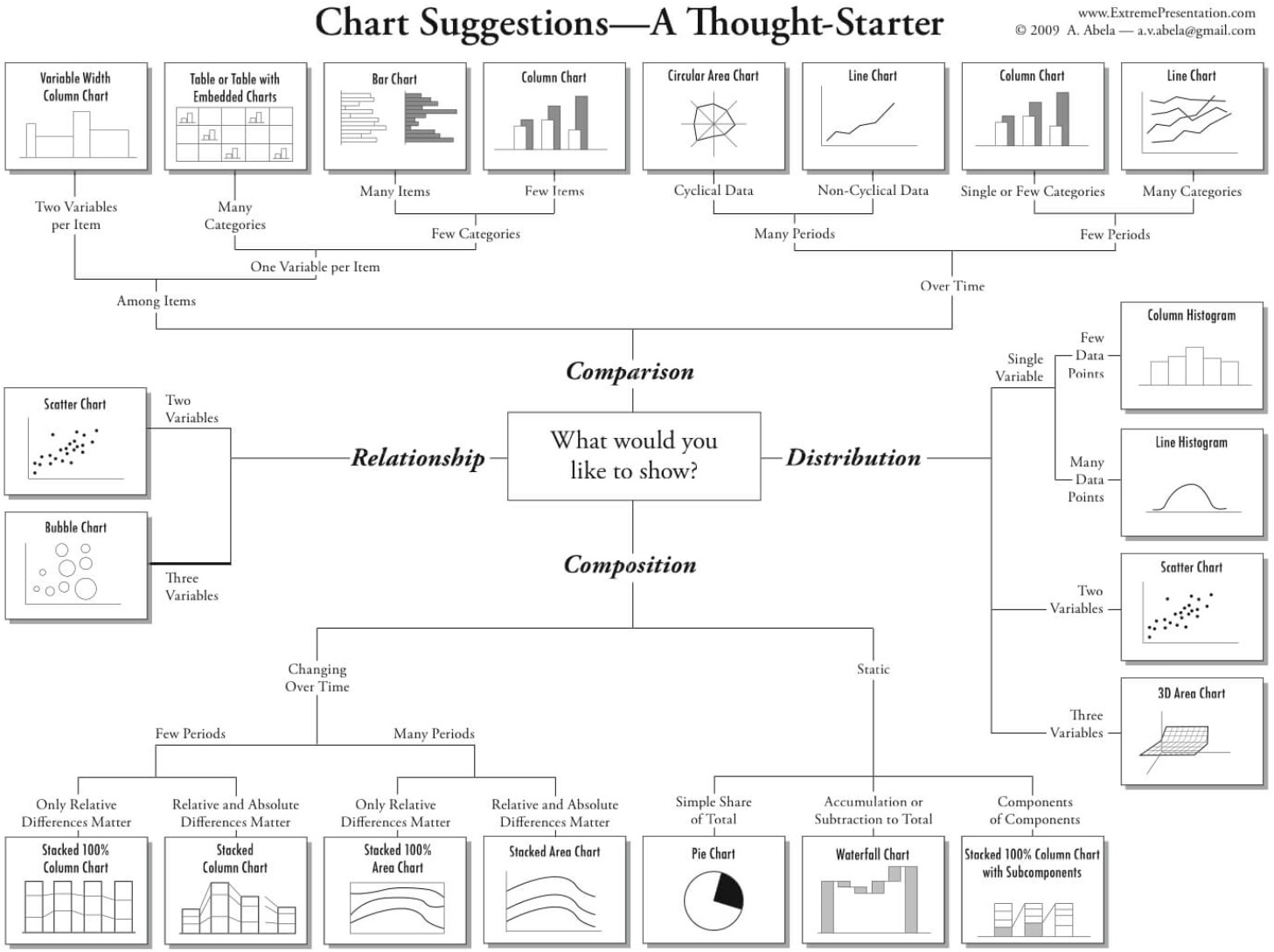
```
# 1個月內(30 days)退貨商品數量的機率分布圖(PDF)
xlab <- vector()
prob <- vector()
for (i in 1:20){
  xlab[i] <- toString(i)
  prob[i] <- dbinom(i, size=30, prob= 2/7)
}

barplot(prob, names.arg = xlab, xlab="退貨商品數", ylab="機率" )
```

1個月內退貨商品數量的機率分布圖



3. 統計圖表



http://extremepresentation.typepad.com/blog/2006/09/choosing_a_good.html

Commonly-used Plots

- Distribution: Histogram; Box plot
- Composition: Pie chart; Stacked bar chart
- Comparison: Bar chart; Box plot
- Relationship: Scatter plot (bubble chart); Heat map

- Combined:
  - Scatter plot + marginal Histogram / Boxplot

Using ggplot2 package

- Based on grammar of graphics (Wilkinson, 2005)
- Plot specification at a high level of abstraction
- It is very flexible
- theme system for polishing plot appearance
- mature and complete graphics system
- many users, active mailing list

Plots: Using ggplot2 package

ggplot(檔名) +aes(欄位設定)

+ geometric objects (geom_) 設定圖表格式

（例如：geom_histogram(),

geom_boxplot()…）

geometric objects (geom_)

Continuous

a <- ggplot(mpg, aes(hwy))

a + **geom_area(stat = "bin")**
x, y, alpha, color, fill, linetype, size
b + geom_area(aes(y = ..density..), stat = "bin")

a + **geom_density(**kernel = "gaussian"**)**
x, y, alpha, color, fill, linetype, size, weight
b + geom_density(aes(y = ..county..))

a + **geom_dotplot()**
x, y, alpha, color, fill

a + **geom_freqpoly()**
x, y, alpha, color, linetype, size
b + geom_freqpoly(aes(y = ..density..))

a + **geom_histogram(**binwidth = 5**)**
x, y, alpha, color, fill, linetype, size, weight
b + geom_histogram(aes(y = ..density..))

Discrete

b <- ggplot(mpg, aes(fl))

b + **geom_bar()**
x, alpha, color, fill, linetype, size, weight

Graphical Primitives

c <- ggplot(map, aes(long, lat))

c + **geom_polygon(**aes(group = group)**)**
x, y, alpha, color, fill, linetype, size

d <- ggplot(economics, aes(date, unemploy))

d + **geom_path(**lineend="butt", linejoin="round', linemitre=1**)**
x, y, alpha, color, linetype, size

Continuous X, Continuous Y

f <- ggplot(mpg, aes(cty, hwy))

f + **geom_blank()**

f + **geom_jitter()**
x, y, alpha, color, fill, shape, size

f + **geom_point()**
x, y, alpha, color, fill, shape, size

f + **geom_quantile()**
x, y, alpha, color, linetype, size, weight

f + **geom_rug(**sides = "bl"**)**
alpha, color, linetype, size

f + **geom_smooth(**model = lm**)**
x, y, alpha, color, fill, linetype, size, weight

f + **geom_text(**aes(label = cty)**)**
x, y, label, alpha, angle, color, family, fontface, hjust, lineheight, size, vjust

Discrete X, Continuous Y

g <- ggplot(mpg, aes(class, hwy))

g + **geom_bar(stat = "identity")**
x, y, alpha, color, fill, linetype, size, weight

g + **geom_boxplot()**
lower, middle, upper, x, ymax, ymin, alpha, color, fill, linetype, shape, size, weight

g + **geom_dotplot(**binaxis = "y", stackdir = "center"**)**
x, y, alpha, color, fill

g + **geom_violin(**scale = "area"**)**

Continuous Bivariate Distribution

i <- ggplot(movies, aes(year, rating))

i + **geom_bin2d(**binwidth = c(5, 0.5)**)**
xmax, xmin, ymax, ymin, alpha, color, fill, linetype, size, weight

i + **geom_density2d()**
x, y, alpha, colour, linetype, size

i + **geom_hex()**
x, y, alpha, colour, fill size

Continuous Function

j <- ggplot(economics, aes(date, unemploy))

j + **geom_area()**
x, y, alpha, color, fill, linetype, size

j + **geom_line()**
x, y, alpha, color, linetype, size

j + **geom_step(**direction = "hv"**)**
x, y, alpha, color, linetype, size

Visualizing error

df <- data.frame(grp = c("A", "B"), fit = 4:5, se = 1:2
k <- ggplot(df, aes(grp, fit, ymin = fit-se, ymax = fit+s

k + **geom_crossbar(**fatten = 2**)**
x, y, ymax, ymin, alpha, color, fill, linetype, size

k + **geom_errorbar()**
x, ymax, ymin, alpha, color, linetype, size, width (also **geom_errorbarh()**)

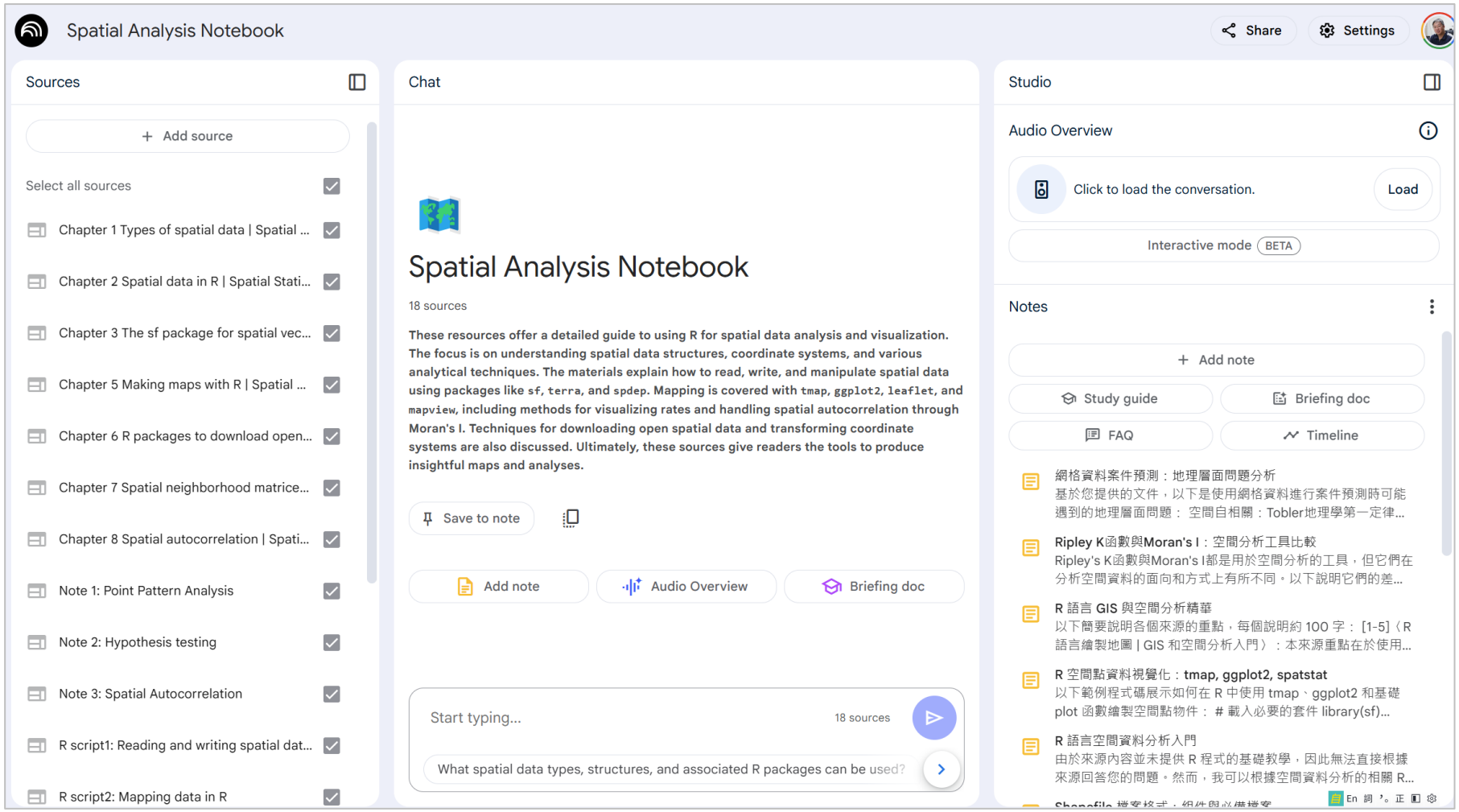
k + **geom_linerange()**
x, ymin, ymax, alpha, color, linetype, size

k + **geom_pointrange()**
x, y, ymin, ymax, alpha, color, fill, linetype, shape, size

課後釋疑問答：Using NotebookLM

填表，提供 gmail address

https://docs.google.com/spreadsheets/d/1SgWy3qtFE0USzHqQhQ4cQIfgd9Fec7eItXV6bzvQ_CM/edit?gid=0#gid=0



本週作業

- **1. 機率分布：**

  (a).某一都市有10萬人口，假設流行一種新興疾病，每人每年被感染機率 p = 0.01，沒有免疫與任何預防措施。請繪製該市的每年感染人數頻率分布圖。

  (b).該市衛生當局定義若某年的感染人數超過960人，該年則視為疫情爆發。市長的任期是4年，若任期內爆發疫情事件，就必須辭職下台。請評估市長在任期四年內，因疫情爆發而辭職的機率?

- **2. 繪製統計圖表與統計檢定 (Student.csv)**

  (a). 比較不同性別(Gender)，讀書時間(StudyHrs)是否有差異？

  (b). 比較不同性別(Gender)，對於虔誠信仰宗教的比例(ReligImp)是否有差異？